

1. The height of a ball in feet x seconds after it is thrown is given by $f(x) = -16x^2 + 32x + 5$.

a. When will the ball reach the ground? $\rightarrow f(x) = 0$

$$0 = -16x^2 + 32x + 5$$

$$\textcircled{1} \quad b^2 - 4ac = (32)^2 - 4(-16)(5) = 1344$$

$$\textcircled{2} \quad x = \frac{-b \pm \sqrt{1344}}{2a} = \frac{-32 \pm \sqrt{1344}}{2(-16)} = \frac{-32 \pm 36.66}{-32}$$

$$\begin{aligned} \frac{-32 + 36.66}{-32} &= -0.15 \\ \text{disregard negative time} \\ \frac{-32 - 36.66}{-32} &= 2.15 \end{aligned}$$

- It will take 2.15 seconds to reach the ground.

b. When will the ball reach a height of 7 feet? $\rightarrow f(x) = 7$

$$\begin{array}{r} 7 = -16x^2 + 32x + 5 \\ -7 \\ \hline 0 = -16x^2 + 32x - 2 \end{array}$$

$$\textcircled{1} \quad b^2 - 4ac = (32)^2 - 4(-16)(-2) = 896$$

$$\textcircled{2} \quad x = \frac{-b \pm \sqrt{896}}{2a} = \frac{-32 \pm \sqrt{896}}{2(-16)} = \frac{-32 \pm 29.93}{-32} \rightarrow \begin{aligned} \frac{-32 + 29.93}{-32} &= 0.06 \\ \frac{-32 - 29.93}{-32} &= 1.94 \end{aligned}$$

- At 0.06 and 1.94 seconds, the ball will be 7 feet high.

2. The fuel economy in miles per gallon of a certain vehicle is given by $f(x) = -0.01x^2 + 1.2x - 5.8$, where x is the car's speed in miles per hour. For what speed(s) does the car have a fuel economy of 22 miles per gallon?

$$\begin{array}{r} 22 = -0.01x^2 + 1.2x - 5.8 \\ -22 \\ \hline 0 = -0.01x^2 + 1.2x - 27.8 \end{array} \quad f(x) = 22$$

$$\textcircled{1} \quad b^2 - 4ac = (1.2)^2 - 4(-0.01)(-27.8) = 0.328$$

$$\textcircled{2} \quad x = \frac{-1.2 \pm \sqrt{0.328}}{2(-0.01)} = \frac{-1.2 \pm 0.57}{-0.02} \rightarrow \begin{aligned} 31.5 \text{ miles per hour} \\ 88.5 \text{ miles per hour} \end{aligned}$$

- If a car goes about 32 mph or 89 mph, it gets 22 miles per gallon.

3. A foul ball leaves the end of a baseball bat and travels according to the formula $h(t) = -16t^2 + 64t$ is the height of the ball in feet and t is the time in seconds.

- a. Find the maximum height reached by the ball.

$$t = -\frac{b}{2a} = -\frac{64}{2(-16)} = \frac{-64}{-32} = 2 \text{ seconds}$$

$$h(t) = -16(2)^2 + 64(2)$$

$$= 64 \text{ ft}$$

At 2 seconds, the ball reaches its max height of 64 feet.

- b. Determine when the foul ball will hit the ground. $h(t) = 0$

$$0 = -16t^2 + 64t$$

$$\textcircled{1} \quad b^2 - 4ac = (64)^2 - 4(-16)(0) = 4096$$

$$\textcircled{2} \quad t = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-64 \pm \sqrt{4096}}{2(-16)} = \frac{-64 \pm 64}{-32}$$

$\rightarrow 0 \text{ seconds}$

$\rightarrow 4 \text{ seconds}$

- The foul ball will reach the ground at 4 seconds.

- c. Determine when the ball will be 48 feet high in the air.

$$h(t) = 48$$

$$\frac{48}{-48} = \frac{-16t^2 + 64t}{-48}$$

$$0 = -16t^2 + 64t - 48$$

$$\textcircled{1} \quad b^2 - 4ac = (64)^2 - 4(-16)(-48) = 1024$$

$$\textcircled{2} \quad t = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-64 \pm \sqrt{1024}}{2(-16)} = \frac{-64 \pm 32}{-32}$$

$\rightarrow 1 \text{ second}$

$\rightarrow 3 \text{ seconds}$

- At 1 second and 3 seconds, the ball will be 48 feet high.